

REGNECENTRALEN

DANSK INSTITUT FOR MATEMATIKMASKINER

ATOMENERGIKOMMISSIONENS

- 3 MAR. 1959

BIBLIOTEK - RISØ

SEKVENS-BETEGNELSE

TF 1

side 1/5

## DASK - BIBLIOTEKSSPECIFIKATION

Kodet af JJ d.12.3.57

Indkørt af JJ d.9.10.57

Udgivet d. 1.10.58

$$y = \sin x$$

$$y = \cos x$$

| Indhops-adresser   | Udhops-adresser | Indgang                        | Udgang                            | Max. ordre-antal | Køretid                                     |                     |
|--------------------|-----------------|--------------------------------|-----------------------------------|------------------|---|---------------------|
|                    |                 |                                |                                   |                  | min.  | max.                |
| 0A8                | 7A8<br>22A8     | C(AR) = x<br>$(-1 \leq x < 1)$ | cos 2πx → AR og MR                | 23               | 85 $\frac{1}{2}$ AT<br>(8 $\frac{1}{2}$ AT) | 87 $\frac{1}{2}$ AT |
| 1A8                |                 |                                | sin 2πx → AR og MR                | 22               | 82 $\frac{1}{2}$ AT<br>(7 $\frac{1}{2}$ AT) | 86 $\frac{1}{2}$ AT |
|                    |                 |                                |                                   |                  |   |                     |
| Kodelængde 0 - 40  |                 |                                |                                   |                  |   |                     |
| Begyndelsesadresse | Lige            |                                | Undersekvenser Ingen              |                  |   |                     |
| Grundparametre     | Ingen           |                                | Arbejdsceller I sekvensen         |                  |   |                     |
| Programparametre   | Ingen           |                                | Perm. konstanter C(2041), C(2043) |                  |   |                     |

## Grundlag

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Sekvensen benytter følgende approksimationspolynomium:

$$\cos 2\pi x = t + t \sum_{n=0}^6 a_n w^n,$$

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$$\text{hvor } w = t^2 - \frac{1}{2}, \quad t = 4(|x| - \frac{1}{2}) - \frac{1}{4},$$

$$\begin{aligned} a_0 &= 0.267\ 162\ 131\ 331 \\ a_1 &= -0.569\ 703\ 680\ 308 \\ a_2 &= 0.072\ 906\ 211\ 195 \\ a_3 &= -0.004\ 369\ 727\ 987 \\ a_4 &= 0.000\ 151\ 654\ 633 \\ a_5 &= -0.000\ 003\ 431\ 829 \\ a_6 &= 0.000\ 000\ 054\ 399 \end{aligned}$$

Endvidere benyttes

$$\sin 2\pi x = \cos 2\pi (x - \frac{1}{4})$$

## Funktion

Sekvensen beregner de trigonometriske funktioner sinus og cosinus.

Sekvensen arbejder med DASK-tal. De resultater, den giver, er alle numerisk mindre end 1, d.v.s. at sekvensen giver

$$\sin \frac{\pi}{2} = \cos 0 = 1 - 2^{-39}$$

$$\sin \frac{3\pi}{2} = \cos \pi = -1 + 2^{-39}$$

Den maksimale fejl er  $6 \cdot 10^{-12}$ .

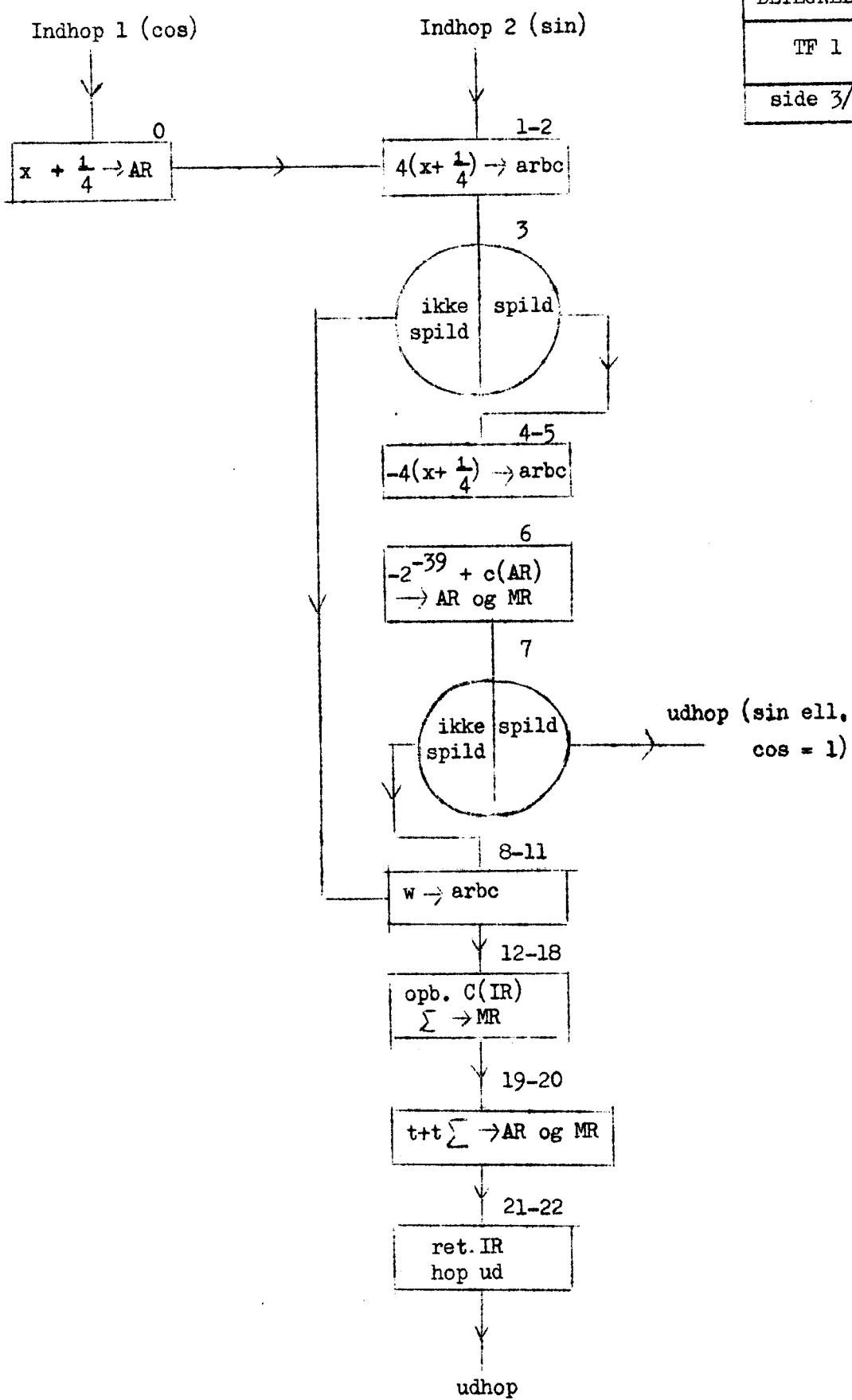
Det bemærkes, at  $C(40A8v) = \frac{1}{4}$ .

(Til forklaring af sekvensens beregning af t skal det nævnes, at formlen for t tankes skrevet således:

$$\begin{aligned} t &= 1 && (x = -1) \\ t &= 4(-x - \frac{1}{4}) = -4(x + \frac{1}{4}) - 2 && (-1 < x < -\frac{1}{2}) \\ t &= 4(x + \frac{1}{4}) && (-\frac{1}{2} \leq x < 0) \\ t &= 1 && (x = 0) \\ t &= 4(-x + \frac{1}{4}) = -4(x + \frac{1}{4}) + 2 && (0 < x < \frac{1}{2}) \\ t &= 4(x - \frac{1}{4}) = 4(x + \frac{1}{4}) - 4 && (\frac{1}{2} \leq x < 1) \end{aligned}$$

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Rutediagram



Kode

|      |        |         |                 | SEKvens-BETEGNELSE  |
|------|--------|---------|-----------------|---|
| cos  | indhop | 0       | 40 A8 20        | $x + \frac{1}{4} \rightarrow AR$  |
| sin  | indhop | 1       | 2 A 0C          | $\left. \begin{array}{l} \\ 4(x+\frac{1}{4}) \end{array} \right\} \rightarrow arbc$           |
|      |        | 2       | 36 A8 08        |   |
|      |        | 8 ← 3   | <u>8 A8 52</u>  | hop, hvis $\frac{1}{2} \leq x \leq 0$ ,   |
|      |        |         | 4 36 A8 41      | $\frac{1}{2} \leq x \leq 1$   |
|      |        |         | 5 36 A8 08      | $\left. \begin{array}{l} \\ -4(x+\frac{1}{4}) \end{array} \right\} \rightarrow arbc$          |
|      |        |         | 6 2041 A 05     | $-2^{-39} + C(AR) \rightarrow AR \text{ og } MR$  |
|      | udhop  | 7       | <u>1 D 12</u>   | hop ud, hvis sin ell. cos = 1   |
|      |        | 3 → 8   | 36 A8 44        | $\left. \begin{array}{l} \\ t^2 \rightarrow AR \end{array} \right\}$                          |
|      |        | 9       | 36 A8 0A        |   |
|      |        | 10      | 2043 A 21       | $\left. \begin{array}{l} \\ w = t^2 - \frac{1}{2} \rightarrow arbc \end{array} \right\}$      |
|      |        | 11      | 38 A8 08        |   |
|      |        | 12      | 23 A8 44        | $a_6 \rightarrow MR$  |
|      |        | 13      | 21 A8 74        | opbevar C(IRD)  |
|      |        | 14      | 2036 A 75       | $-12 \rightarrow IRD \quad (0 \Rightarrow j)$   |
|      |        | 18 → 15 | 2 D 75          | $2 + \sum_j C(IRD) \rightarrow IRD \quad (j+1 \Rightarrow j)$                                 |
|      |        | 16      | 38 A8 0A        | $\left. \begin{array}{l} \\ \sum_{n=0}^j a_{6-n} w^{j-n} \rightarrow MR \end{array} \right\}$ |
|      |        | 17      | 34 D8 04        |   |
|      |        | 15 ← 18 | <u>15 A8 73</u> | hop, hvis $j \leq 6$  |
|      |        | 19      | 36 A8 0A        | $\left. \begin{array}{l} \\ t+t \sum \rightarrow AR \text{ og } MR \end{array} \right\}$      |
|      |        | 20      | 36 A8 04        |   |
| (13) |        | 21      | (0) A 75        | retabler IRD  |
|      | udhop  | 22      | <u>1 D 10</u>   | hop ud  |
|      |        | 23      | B 074D2         | $a_6$   |
|      |        | 24      | B FFFE          | $\left. \begin{array}{l} \\ a_5 \end{array} \right\}$   |
|      |        | 25      | B 33634         |   |
|      |        | 26      | B 0004F         | $\left. \begin{array}{l} \\ a_4 \end{array} \right\}$   |
|      |        | 27      | B 82BD8         |   |
|      |        | 28      | B FF70D         | $\left. \begin{array}{l} \\ a_3 \end{array} \right\}$   |
|      |        | 29      | B 0109A         |   |
|      |        | 30      | B 0954F         | $\left. \begin{array}{l} \\ a_2 \end{array} \right\}$   |
|      |        | 31      | B DA061         |   |
|      |        | 32      | B B713F         | $\left. \begin{array}{l} \\ a_1 \end{array} \right\}$   |
|      |        | 33      | B 32655         |   |

Kode

|    |   |       |
|----|---|-------|
| 34 | B | 22325 |
| 35 | B | E6466 |
| 36 | A |       |
| 37 | A |       |
| 38 | A |       |
| 39 | A |       |
| 40 | B | 20000 |

$\left. \begin{array}{l} \\ \\ \\ \\ \\ \end{array} \right\} a_0$   
 $\left. \begin{array}{l} \\ \\ \\ \\ \end{array} \right\} abc$   
 $\frac{1}{4}$

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